

# Robust Unsupervised Audio-visual Speech Enhancement Using a Mixture of Variational Autoencoders

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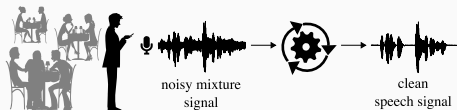
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# Introduction

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# Unsupervised speech enhancement



In the short-time Fourier transform (STFT) domain, for all  $(f, n) \in \mathbb{B} = \{0, \dots, F - 1\} \times \{0, \dots, N - 1\}$ , we observe:

$$x_{fn} = s_{fn} + b_{fn},$$

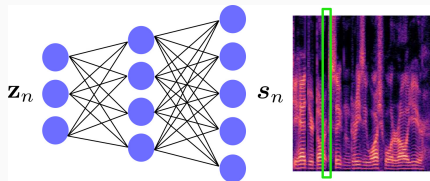
- $s_{fn}$  is the **clean speech signal**.
- $b_{fn}$  is the **noise signal**.
- $f$  is the frequency index and  $n$  the time-frame index.

*Separate the speech and noise signals from the observed mixture signal without training on noise.*

# Generative speech model [Bando et al., 2018; Leglaive et al., 2018]

Generative model for each clean spectrogram time frame  $s_n$ :

$$s_n | \mathbf{z}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^a(\mathbf{z}_n))), \quad \text{with } \mathbf{z}_n \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$



- $\mathbf{z}_n \in \mathbb{R}^L$  is a latent random variable ( $L \ll F$ )
- $\boldsymbol{\sigma}_s^a(\cdot) : \mathbb{R}^L \mapsto \mathbb{R}_+^F$  is a neural network parameterized by  $\boldsymbol{\theta}$

*Estimate the generative model parameters, i.e.  $\boldsymbol{\theta}$ .*

## Learning the parameters

- **Training dataset** of STFT speech time frames:  $\mathbf{s} = \{\mathbf{s}_n \in \mathbb{C}^F\}_{n=0}^{N_{tr}-1}$
- **Difficulty:** Intractable likelihood  $p(\mathbf{s}; \boldsymbol{\theta}) = \int p(\mathbf{s}|\mathbf{z}; \boldsymbol{\theta})p(\mathbf{z})d\mathbf{z}$
- **Solution:** **Variational autoencoder** (VAE) [Kingma and Welling 2014]

Using **variational inference**, maximize a lower bound of  $\ln p(\mathbf{s}; \boldsymbol{\theta})$ :

$$\mathcal{L}(\boldsymbol{\theta}, \boldsymbol{\psi}) = \frac{1}{N_{tr}} \sum_{n=0}^{N_{tr}-1} \mathbb{E}_{q(\mathbf{z}_n|\mathbf{s}_n; \boldsymbol{\psi})} \left[ \ln p(\mathbf{s}_n|\mathbf{z}_n; \boldsymbol{\theta}) \right] - D_{\text{KL}}\left(q(\mathbf{z}_n|\mathbf{s}_n; \boldsymbol{\psi}) \parallel p(\mathbf{z}_n)\right)$$

where  $q(\mathbf{z}_n|\mathbf{s}_n; \boldsymbol{\psi}) \approx p(\mathbf{z}_n|\mathbf{s}_n; \boldsymbol{\theta})$  is defined by an “encoding network” with parameters  $\boldsymbol{\psi}$ .  $D_{\text{KL}}(\cdot \parallel \cdot)$  is the Kullback–Leibler divergence.

# Speech enhancement

**Noisy speech model:**  $\forall n : \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$

**Noise model:**  $\forall n : \mathbf{b}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n]))$

**Clean speech model:** Trained VAE

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▷ Observed variables:  $\mathbf{x} = \{\mathbf{x}_n\}_{n=0}^{N-1}$ . Latent variables:  $\mathbf{z} = \{\mathbf{z}_n\}_{n=0}^{N-1}$

▷ Parameters to be estimated:  $\theta_u = \{\mathbf{W}_b, \mathbf{H}_b\}$

## Monte-Carlo Expectation maximization (MCEM):

- **E-Step:**  $Q(\theta_u; \theta_u^*) = \mathbb{E}_{p(\mathbf{z}|\mathbf{x}; \theta_u^*)}[\ln p(\mathbf{x}, \mathbf{z}; \theta, \theta_u)]$ .
- **M-Step:**  $\theta_u^* \leftarrow \arg \max_{\theta_u} Q(\theta_u; \theta_u^*)$ .

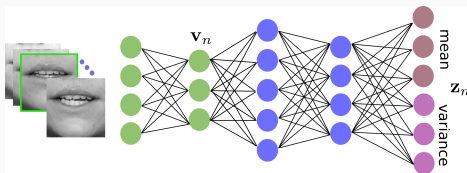
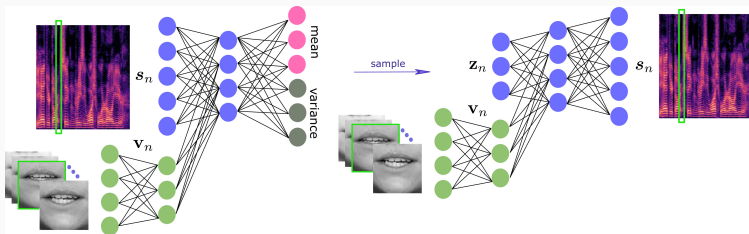
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## Speech estimation:

$$\hat{s}_{fn} = \mathbb{E}_{p(s_{fn}|x_{fn}; \theta^*)}[s_{fn}] = \mathbb{E}_{p(\mathbf{z}_n|\mathbf{x}_n; \theta^*)} \left[ \mathbb{E}_{p(s_{fn}|\mathbf{z}_n, \mathbf{x}_n; \theta^*)}[s_{fn}] \right]$$

# Audio-visual modeling of clean speech [Sadeghi et al., 2019]

- Generative model:  $p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n) = \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^{av}(\mathbf{z}_n, \mathbf{v}_n)))$
- Encoder:  $q(\mathbf{z}_n | \mathbf{s}_n, \mathbf{v}_n; \boldsymbol{\psi}) = \mathcal{N}(\boldsymbol{\mu}_z^{av}(\mathbf{s}_n, \mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z^{av}(\mathbf{s}_n, \mathbf{v}_n)))$
- Prior of  $\mathbf{z}_n$ :  $p(\mathbf{z}_n | \mathbf{v}_n) = \mathcal{N}(\boldsymbol{\mu}_z(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z(\mathbf{v}_n)))$



# **Robust Audio-visual Speech Enhancement**

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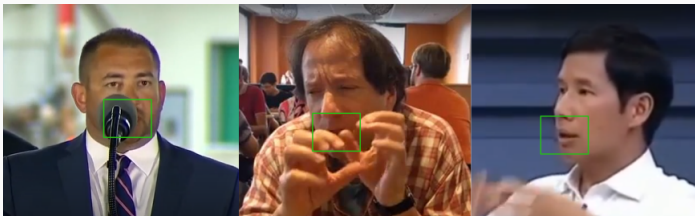


# Introduction

AV-VAE usually yields better results than A-VAE, especially at low SNRs, provided **clean (frontal, non-occluded)** visual data [Sadeghi et al., 2019].

## Noisy visual data:

Some video frames might contain occluded and/or non-frontal lips region.

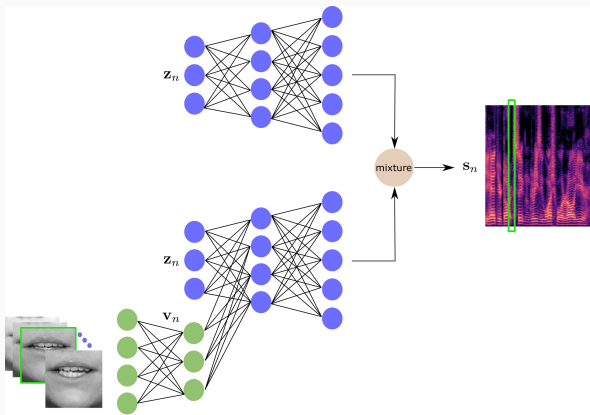


*How to effectively benefit from AV-VAE for in-the-wild video recordings?*

# Our work: VAE mixture model (VAE-MM)

A **mixture** of A-VAE plus AV-VAE generative model:

- If the lips region is clean, use AV-VAE, otherwise use A-VAE.



The A-VAE and AV-VAE have been already trained on clean data.

# Generative model

**Mixture generative model:** Combine A-VAE with AV-VAE

$$\begin{cases} p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n, \alpha_n) &= \left[ \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^a(\mathbf{z}_n))) \right]^{\alpha_n} \times \left[ \mathcal{N}_c(\mathbf{0}, \text{diag}(\boldsymbol{\sigma}_s^{av}(\mathbf{z}_n, \mathbf{v}_n))) \right]^{1-\alpha_n} \\ p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) &= \left[ \mathcal{N}(\mathbf{0}, \mathbf{I}) \right]^{\alpha_n} \times \left[ \mathcal{N}(\boldsymbol{\mu}_z^v(\mathbf{v}_n), \text{diag}(\boldsymbol{\sigma}_z^v(\mathbf{v}_n))) \right]^{1-\alpha_n}, \\ p(\alpha_n) &= \pi^{\alpha_n} \times (1 - \pi)^{1-\alpha_n}. \end{cases}$$

$\alpha_n \in \{0, 1\}$  is a latent variable specifying the component of the mixture model that is used by the  $n$ -th frame.

# Parameter estimation

**Noisy speech model:**  $\forall n : \mathbf{x}_n = \mathbf{s}_n + \mathbf{b}_n$

**Noise model:**  $\forall n : \mathbf{b}_n \sim \mathcal{N}_c(\mathbf{0}, \text{diag}(\mathbf{W}_b \mathbf{H}_b[:, n]))$

**Clean speech model:** Trained A-VAE and AV-VAE generative networks

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## Inference:

- ▷ Observed variables:  $\{\mathbf{x}_n, \mathbf{v}_n\}_{n=0}^{N-1}$
- ▷ Latent variables:  $\{\mathbf{s}_n, \mathbf{z}_n, \alpha_n\}_{n=0}^{N-1}$
- ▷ Parameters to be estimated:  $\boldsymbol{\theta}_u = \{\mathbf{W}_b, \mathbf{H}_b, \pi\}$

# Parameter estimation

## Variational Expectation-maximization (VEM)

### Variational E-Step:

The intractable posterior  $p(\mathbf{s}_n, \mathbf{z}_n, \alpha_n | \mathbf{x}_n, \mathbf{v}_n; \boldsymbol{\theta}_u)$  is approximated by a variational distribution factorizing as follows:

$$r(\mathbf{s}_n, \mathbf{z}_n, \alpha_n) = r(\mathbf{s}_n) r(\mathbf{z}_n) r(\alpha_n),$$

which are updated as follows [Bishop, 2006]:

VE  $\mathbf{s}_n$ -step:  $r(\mathbf{s}_n) \propto \exp \left( \mathbb{E}_{r(\mathbf{z}_n) \cdot r(\alpha_n)} \left[ \log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

VE  $\mathbf{z}_n$ -step:  $r(\mathbf{z}_n) \propto \exp \left( \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\alpha_n)} \left[ \log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

VE  $\alpha_n$ -step:  $r(\alpha_n) \propto \exp \left( \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[ \log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \right)$

## VE $s_n$ -step

$$r(\mathbf{s}_n) = \mathcal{N}_c(\mathbf{m}_n, \text{diag}(\boldsymbol{\nu}_n)), \quad \begin{cases} m_{fn} &= \frac{\gamma_{fn}}{\gamma_{fn} + (\mathbf{W}_b \mathbf{H}_b)_{fn}} \cdot x_{fn} \\ \nu_{fn} &= \frac{\gamma_{fn} \cdot (\mathbf{W}_b \mathbf{H}_b)_{fn}}{\gamma_{fn} + (\mathbf{W}_b \mathbf{H}_b)_{fn}} \end{cases}$$

which can be interpreted as an **averaged Wiener filtering**.

$$\gamma_{fn}^{-1} = \sum_{\alpha_n \in \{0,1\}} r(\alpha_n) \cdot \eta_{fn}^{\alpha_n} \quad (\text{weighted precision over audio and audio-visual cases}),$$

$$\eta_{fn}^{\alpha_n} = \mathbb{E}_{r(\mathbf{z}_n)} \left[ \frac{1}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n)} \right] \approx \frac{1}{D} \sum_{d=1}^D \frac{1}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n^{(d)}, \mathbf{v}_n)} \quad (\text{average precision}),$$

and  $\{\mathbf{z}_n^{(d)}\}_{d=1}^D$  is a sequence sampled from  $r(\mathbf{z}_n)$ . Moreover:

$$\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n) = \begin{cases} \sigma_{s,f}^a(\mathbf{z}_n) & \alpha_n = 1 \\ \sigma_{s,f}^{av}(\mathbf{z}_n, \mathbf{v}_n) & \alpha_n = 0 \end{cases}.$$

For  $r(\mathbf{z}_n)$  we obtain the following result:

$$r(\mathbf{z}_n) \propto \exp \left( \sum_{\alpha_n \in \{0,1\}} r(\alpha_n) \cdot \left[ \log p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) + \sum_f -\log \left( \sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n) \right) - \frac{|m_{fn}|^2 + \nu_{fn}}{\sigma_{s,f}^{\alpha_n}(\mathbf{z}_n, \mathbf{v}_n)} \right] \right).$$

The above distribution cannot be computed in closed-form. Nevertheless, we can draw samples from it using the **Metropolis-Hastings** (MH) algorithm (see our paper for more details).

To update the variational distribution of  $\alpha_n$ , we can write:

$$r(\alpha_n) \propto \exp \left( \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[ \log p(\mathbf{s}_n | \mathbf{z}_n, \mathbf{v}_n, \alpha_n) + \log p(\mathbf{z}_n | \mathbf{v}_n, \alpha_n) + \log p(\alpha_n) \right] \right)$$

which is a Bernoulli distribution with

$$\pi_n = g \left( \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n)} \left[ \log \frac{p(\mathbf{s}_n, \mathbf{z}_n | \mathbf{v}_n, \alpha_n = 1)}{p(\mathbf{s}_n, \mathbf{z}_n | \mathbf{v}_n, \alpha_n = 0)} \right] + \log \frac{\pi}{1 - \pi} \right)$$

as the parameter, which is an **averaged audio/audio-visual ratio**. Here,  $g(\cdot)$  denotes the sigmoid function defined as  $g(x) = 1/(1 + \exp(-x))$ .



# Parameters update and speech enhancement

## M-Step:

Update parameters by optimizing the complete data log-likelihood:

$$\begin{aligned} Q(\boldsymbol{\theta}_u, \boldsymbol{\theta}_u^{\text{old}}) &\stackrel{c}{=} \mathbb{E}_{r(\mathbf{s}_n) \cdot r(\mathbf{z}_n) \cdot r(\alpha_n)} \left[ \log p(\mathbf{x}_n, \mathbf{s}_n, \mathbf{z}_n, \alpha_n, \mathbf{v}_n; \boldsymbol{\theta}_u) \right] \\ &\stackrel{c}{=} \mathbb{E}_{r(\mathbf{s}_n)} \left[ \log p(\mathbf{x}_n | \mathbf{s}_n; \boldsymbol{\theta}_u) \right] + \mathbb{E}_{r(\alpha_n)} \left[ \log p(\alpha_n) \right] \\ &\stackrel{c}{=} \sum_{f,n} -\log (\mathbf{W}_b \mathbf{H}_b)_{fn} - \left( \frac{|x_{fn} - m_{fn}|^2 + \nu_{fn}}{(\mathbf{W}_b \mathbf{H}_b)_{fn}} \right) + \pi_n \log \pi + (1 - \pi_n) \end{aligned}$$

## Speech enhancement:

After the convergence of the VEM, the speech STFT frames are estimated using an **averaged Wiener filtering**:

$$\hat{s}_{fn} = \mathbb{E}_{r(s_{fn})} [s_{fn}] = \frac{\gamma_{fn}^*}{\gamma_{fn}^* + (\mathbf{W}_b^* \mathbf{H}_b^*)_{fn}} \cdot x_{fn} \quad \forall (f, n)$$

# Experiments

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# Dataset

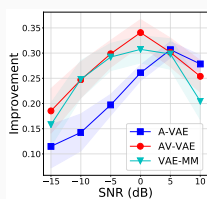
- **Noisy+clean speech:** NTCD-TIMIT database [Abdelaziz, 2017]
- **VAE models:** Pre-trained A-VAE and AV-VAE [Sadeghi et al., 2019]
- **Setup:**
  - Testing set of NTCD-TIMIT database;
  - $\sim$  1 hours of speech;
  - 9 speakers;
  - Noise types: *LR, White, Cafe, Car, Babble, and Street*;
  - Noise levels:  $-15, -10, -5, 0, 5, 10$  dB;
  - 270 noisy mixtures per noise level;
  - **Different speakers and sentences** than in the training set;
  - Clean lips region as well as noisy versions ( $\sim$  one-third of total video frames/sample)

# Results

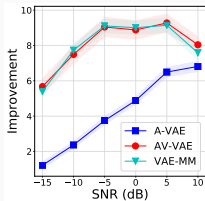
Objective measures (the higher, the better)

- Signal-to-distortion ratio (SDR).
- Perceptual evaluation of speech quality (PESQ) measure.

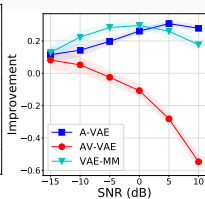
Improvement with respect to the input:



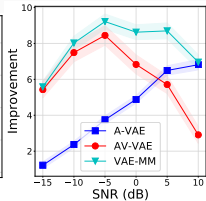
(a) PESQ(clean)



(b) SDR(clean)



(c) PESQ(noisy)



(d) SDR(noisy)

## Conclusion and future work

*The proposed robust technique can efficiently benefit from visual data for speech enhancement when some lips region frames are noisy (non-frontal, occluded).*

- The VEM framework is slow. Trying to re-use the trained encoders at inference time can reduce the complexity.
- Temporal modeling of the latent variables to benefit from time dependency between audio as well as visual frames.

Thank you for your attention

## References

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